

# Higgs Couplings at Muon Colliders with Delphes

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# Single Higgs Production at Muon Colliders

First look at single Higgs precision for a 10 TeV muon collider ( $\mathcal{L} = 10\text{ab}^{-1}$ ) was in the Muon Smasher's Guide (2103.14043)

- Looked at most relevant channels, but was **signal only**

Here we show our preliminary results for most relevant channels including physics backgrounds at 3 TeV ( $1\text{ ab}^{-1}$ ) and 10 TeV ( $10\text{ ab}^{-1}$ ) using Delphes fast simulation

Full simulation studies are under way for several processes (i.e. Higgs 2021: L. Giambastiani, G. Da Molin), but only up to 3 TeV and won't cover all relevant channels.

$b\bar{b}$  and  $WW^* \rightarrow jj\ell\nu$  (L. Sestini et. al.) will hopefully be key points of comparison for us

# Event Generation and Detector Assumptions

Event generation is done mostly using MadGraph5 and showering with Pythia8

Require final state  $p_{T,\mu} > 10$  GeV for  $ZZ/Z\gamma/\gamma\gamma F$  and  $WZ/W\gamma F$  processes to avoid singularities

Use DELPHES fast muon collider card for the detector:

Hybrid of FCC-hh and CLIC detector cards for efficiencies and reconstruction<sup>1</sup>

Limits detectors to  $|\eta| < 2.5$  roughly corresponding to BIB reducing tungsten nozzles with opening  $\theta \approx 10^\circ$

Includes hypothetical forward muon detector from  $2.5 < |\eta| < 8.0$  with 10% energy resolution

<sup>1</sup>[https://indico.cern.ch/event/957299/contributions/4023467/attachments/2106044/3541874/delphes\\_card\\_mucol\\_mdi\\_.pdf](https://indico.cern.ch/event/957299/contributions/4023467/attachments/2106044/3541874/delphes_card_mucol_mdi_.pdf)

# Flavour Tagging

*b*-tagging is done using the tight working point (50%) inspired by CLIC (1812.07337)

- *c*-quark mis-tagging rate  $\leq 3\%$
- light quark mistagging rate  $\leq 0.5\%$

For *c*-tagging, we use the tagging rates of ILC reported in (1506.08371). We take 20% as our working point to match the Smasher's Guide.

- *b*-mistagging rate of flat 1.3%
- light quark mistagging rate of flat 0.66%

We note that the worse mistag rates of the original CLIC design report (1202.5940) yield very similar results.

# Event Reconstruction

Events are subject to the same cuts and jet clustering as done in the Smasher's Guide.

We use the Valencia jet clustering algorithm with  $\beta = \gamma = 1$  (1607.05039).

Events are clustered in exclusive mode with  $R = 0.5$

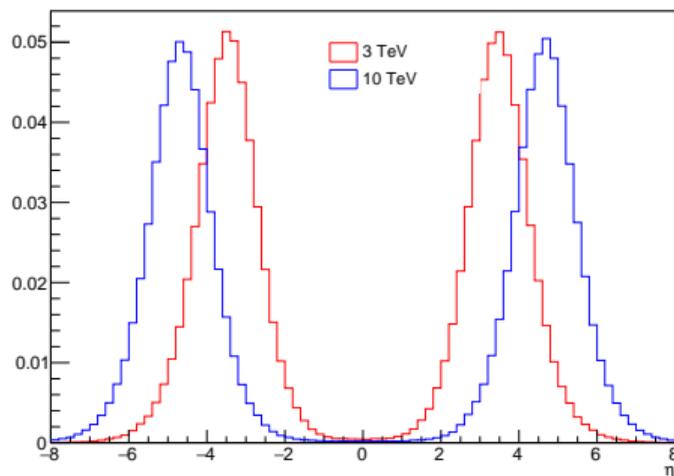
2-body final states required to have both particles satisfying  $|\eta| < 2.5$  and  $P_T > 40$  GeV.

For 4-body final states, loosen the  $P_T$  cut to 20 GeV.

Apply additional process dependent cuts, estimate precision using  $\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{N_{sig} + N_{bkg}}}{N_{sig}}$

# Forward Muons

To distinguish between  $W$ -fusion and  $Z$ -fusion, must be able to tag the forward muons beyond the  $|\eta| \approx 2.5$  nozzles



For  $b\bar{b}$ , we include additional results assuming the ability to tag these forward muons. **These are a work in progress and idealised at the moment.**

# Event Selection ( $b\bar{b}$ , $c\bar{c}$ , $gg(+s\bar{s})$ )

Apply an additional correction to  $b$ -jet  $p_T$  to account for energy losses during reconstruction (1811.02572)

- Smoothly scales 4-momentum by up to  $\sim 1.16$  at low  $p_T$
- Rough approximation to ATLAS  $ptcorr$  correction (1708.03299)
- Reproduces a Higgs peak centered near 125 GeV

Apply a similar correction to  $c$ -jets

Events that pass the  $P_T$  and  $\eta$  cuts are then selected based on an invariant mass cut:

- $100 < M_{b\bar{b}} < 150$  for  $b\bar{b}$
- $105 < M_{c\bar{c}} < 145$  for  $c\bar{c}$
- $95 < M_{jj} < 135$  for  $gg(+s\bar{s})$

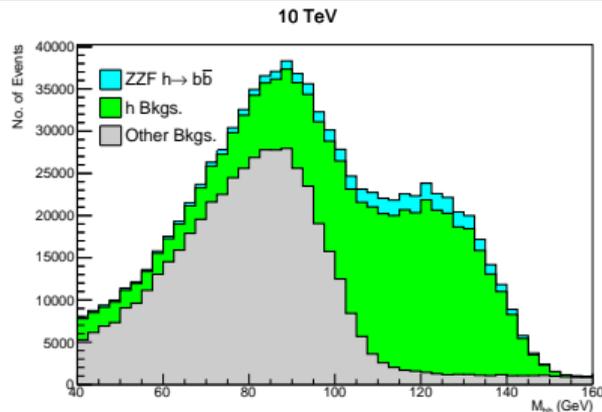
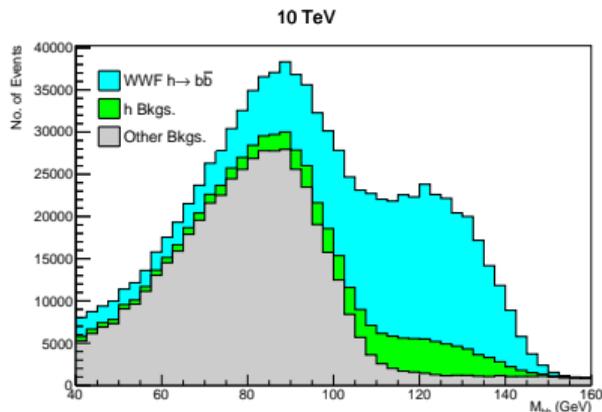
# Backgrounds ( $b\bar{b}$ )

Primary backgrounds: 10 TeV at  $10\text{ab}^{-1}$

Process	$\sigma$ (fb)	$A \cdot \epsilon$ (%)	Events
$\mu^+\mu^- \rightarrow \nu_\mu\bar{\nu}_\mu H; H \rightarrow b\bar{b}$	490	5.2	250000
$\mu^+\mu^- \rightarrow b\bar{b}(\nu\nu, \mu\mu)$	620	0.56	34000
$\mu^+\mu^- \rightarrow \mu^+\mu^- H; H \rightarrow b\bar{b}$	50	5.2	27000
$\mu\nu WH; H \rightarrow b\bar{b}$	41	4.0	16000
$(\mu\mu, \nu\nu)ZH; H \rightarrow b\bar{b}$	21	4.2	8600
Others	-	-	11000

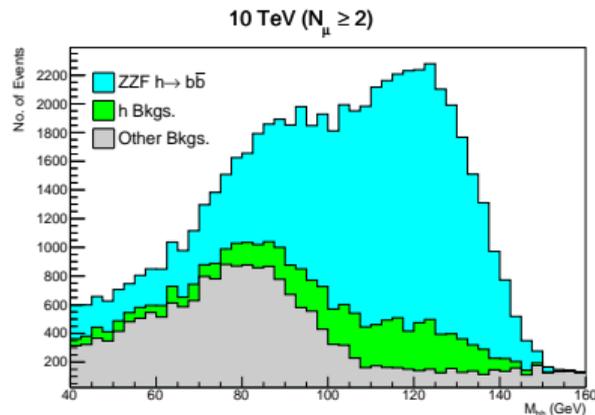
Where others includes VBF  $WZ$ ,  $ZZ$ ,  $t\bar{b}$ ,  $t\bar{t}$ , and  $HH$

# $b\bar{b}$ at 10 TeV



Precision (%)

Energy	WWF	ZZF	ZZF ( $N_{\mu} \geq 2$ )
3 TeV	0.84	7.9	2.5
10 TeV	0.24	2.2	0.73



# $c\bar{c}, gg(+s\bar{s})$

The dominant backgrounds for  $c\bar{c}$  and  $gg(+s\bar{s})$  are mostly the same as for  $b\bar{b}$  and primarily removed via the  $M_{jj}$  cut

Invariant mass resolution critical for distinguishing  $Z$ (and  $W$ ) peaks from the  $H$

$H \rightarrow b\bar{b}$  becomes a large irreducible background

Following the same procedure as in  $b\bar{b}$ , we obtain results for  $c\bar{c}$  and  $gg(+s\bar{s})$  :

Energy	Precision (%)	
	$c\bar{c}$	$gg(+s\bar{s})$
3 TeV	14	4.2
10 TeV	4.4	1.2

For  $H \rightarrow \tau\tau$ , we take a  $\tau$ -tagging efficiency of 80% with a jet mistag rate of 2%

Energy losses due to neutrinos in  $\tau$ -decays make an invariant mass cut alone less useful.

Since all  $W$ -fusion carries lots of missing energy, MET is likewise not very useful

We find a  $80 < M_{\tau\tau} < 130$  cut combined with  $\theta_{\tau\tau} > 20(15)$  at 3(10) TeV cuts down the dominant  $\mu\mu \rightarrow (\nu\nu, \mu\mu)\tau\tau$  background substantially

We find a precision of 4.5% at 3 TeV and 1.3% at 10 TeV

$$WW^* \rightarrow jj\ell\nu$$

For  $WW^*$  and  $ZZ^*$ , we generate the full  $2 \rightarrow 6$  backgrounds such as  $\mu\mu \rightarrow \nu\nu\ell\ell jj$  using MadGraph.

For  $WW^* \rightarrow jj\nu\ell$ , the story is much the same as  $\tau\tau$ , as the full  $M_H$  cannot be fully reconstructed.

We require two jets and one isolated lepton and apply the mass cuts:

- $5 < M_{jj} < 90$
- $20 < M_{jj\ell} < 110$
- $40 < E_{jj} < 700, 85 < E_{jj\ell} < 800$  (3 TeV)
- $50 < E_{jj} < 1100, 90 < E_{jj\ell} < 1600$  (10 TeV)

We find the majority of the background is removed using these cuts

Precision:

- 1.79% (3 TeV)
- 0.48% (10 TeV)

$$ZZ^* \rightarrow jj\ell\ell$$

We apply the cuts:

- $5 < M_{Z^*} < 60$
- $15 < M_Z < 100$
- $50 < M_H < 135$  ( $Z \rightarrow jj, Z^* \rightarrow \ell\ell$ )
- $80 < M_H < 130$  ( $Z^* \rightarrow jj, Z \rightarrow \ell\ell$ )

Thanks to the lepton pair, this channel is clean, but statistically limited

Process	No. of Events	
	3 TeV	10 TeV
$\nu\nu H \rightarrow \nu\nu\ell\ell jj$	103	1590
Other VBF Higgs	14	207
$(\ell\ell, \tau\tau)\nu\nu jj$	25	901
$\ell\ell\nu\ell jj, t\bar{t}, tb$	15	244

Overall we find a precision of 12% at 3 TeV and 3.4% at 10 TeV.

For  $\gamma\gamma$ , ISR becomes very important, so we include it in event generation by using Whizard.

Require no isolated leptons and a cut of  $122 < M_{\gamma\gamma} < 128$

Process	No. of Events	
	3 TeV	10 TeV
$\nu\nu H \rightarrow \nu\nu\gamma\gamma$	415	5590
$\mu\mu H \rightarrow \mu\mu\gamma\gamma$	34	583
$\nu\nu\gamma\gamma$	321	3890
$\nu\nu\gamma(+ISR)$	264	3290
$\mu\mu\gamma\gamma$	7	35
$\mu\mu\gamma(+ISR)$	38	425

Find a precision of 7.9% at 3 TeV and 2.1% at 10 TeV.

This channel has been analysed at 3 TeV using full simulation<sup>1</sup> (A. Montella), obtaining 38% precision.

For our case, we do a very simple analysis using fastsim:

Require 2 isolated muons with  $P_T > 20$ ,  $|\eta| < 2.5$ ,

Keep events passing a cut of  $124 < M_{\mu\mu} < 126$

We find a precision of 44% at 3 TeV and 11% at 10 TeV.

<sup>1</sup>[https://indico.cern.ch/event/1030068/contributions/4513645/attachments/2329111/3968454/montella\\_Higgs\\_2021.pdf](https://indico.cern.ch/event/1030068/contributions/4513645/attachments/2329111/3968454/montella_Higgs_2021.pdf)

Production	Decay	Rate [fb]	$A \cdot \epsilon$ [%]	$\Delta\sigma/\sigma$ [%]	Signal Only $\Delta\sigma/\sigma$ [%]
W-fusion	$bb$	485	5.2	0.24	0.17
	$cc$	24.4	0.83	4.4	1.7
	$gg(+ss)$	72.2	14	1.2	0.19
	$\tau^+\tau^-$	53.1	3.2	1.3	0.54
	$WW^*(jj\ell\nu)$	52.8	17	0.48	0.30
	$ZZ^*(jj\ell^+\ell^-)$	2.07	7.7	3.4	2.3
	$\gamma\gamma$	1.92	29	2.1	1.3
	$\mu^+\mu^-$	0.18	39	11	0.37
Z-fusion	$bb$	49.6	5.4	2.2	0.49
	$bb (N_\mu \geq 2)$	49.6	4.9	0.73	

## Preliminary

Production	Decay	$\Delta\sigma/\sigma$ (%)	
		3 TeV	10 TeV
W-fusion	$bb$	0.84	0.24
	$cc$	14	4.4
	$gg(+ss)$	4.2	1.2
	$\tau^+\tau^-$	4.5	1.3
	$WW^*(jjl\nu)$	1.8	0.48
	$ZZ^*(jjll)$	12	3.4
	$\gamma\gamma$	7.9	2.1
	$\mu^+\mu^-$	44	11
Z-fusion	$bb$	7.9	2.2
	$bb (N_\mu \geq 2)$	2.5	0.73

### Preliminary Fit Result [%]

	3 TeV @ 1 ab <sup>-1</sup>	10 TeV @ 10 ab <sup>-1</sup>
$\kappa_W$	0.45	0.13
$\kappa_Z$	3.4	0.96
$\kappa_g$	2.4	0.68
$\kappa_\gamma$	4.0	1.1
$\kappa_{Z\gamma}$	–	–
$\kappa_c$	7.4	2.3
$\kappa_t$	–	–
$\kappa_b$	0.99	0.28
$\kappa_\mu$	22	5.3
$\kappa_\tau$	2.5	0.71

Where – means it was fixed to the SM (relevant channel still in progress).

**Preliminary** Fit Result 10 TeV @ 10 ab<sup>-1</sup> [%]

	10 TeV Muon Collider	with HL-LHC	with HL-LHC + 250 GeV e <sup>+</sup> e <sup>-</sup>
$\kappa_W$	0.13	0.12	0.11
$\kappa_Z$	0.96	0.77	0.11
$\kappa_g$	0.68	0.64	0.50
$\kappa_\gamma$	1.1	0.84	0.81
$\kappa_{Z\gamma}$	–	–	4.1
$\kappa_c$	2.3	2.3	1.4
$\kappa_t$	–	3.2	3.2
$\kappa_b$	0.28	0.27	0.23
$\kappa_\mu$	5.3	3.6	3.3
$\kappa_\tau$	0.71	0.64	0.43

# Future Plans

We are finishing the last few relevant channels and should be done soon. Plan to add:

- $WW^* \rightarrow 4j$
- $ZZ^* \rightarrow 4j, 4\ell$
- $Z(jj)\gamma$
- $t\bar{t}H$

Detailed comparison of these results to full sim still needs to be done for validation.

- However, we have tried to remain conservative with respect to BIB

Next step- measurement of the Higgs width

# BACKUPS

**Preliminary 3 TeV @ 1 ab<sup>-1</sup>**

Production	Decay	Rate [fb]	$A \cdot \epsilon$ [%]	$\Delta\sigma/\sigma$ [%]
W-fusion	$bb$	287	6.6	0.84
	$cc$	14.5	1.1	14
	$gg(+ss)$	42.8	17	4.2
	$\tau^+\tau^-$	31.5	3.9	4.5
	$WW^*(jjl\nu)$	31.3	20	1.8
	$ZZ^*(jjl^+l^-)$	1.23	8.4	12
	$\gamma\gamma$	1.14	37	4.9
	$\mu^+\mu^-$	0.11	52	44
Z-fusion	$bb$	29.3	6.8	7.9
	$bb (N_\mu \geq 2)$	29.3	6.2	2.5

**Preliminary** Fit Result 3 TeV @ 1 ab<sup>-1</sup> [%]

	3 TeV Muon Collider	with HL-LHC	with HL-LHC + 250 GeV e <sup>+</sup> e <sup>-</sup>
$\kappa_W$	0.45	0.40	0.33
$\kappa_Z$	3.4	1.3	0.12
$\kappa_g$	2.4	1.5	0.74
$\kappa_\gamma$	4.0	1.3	1.2
$\kappa_{Z\gamma}$	–	–	4.2
$\kappa_c$	7.4	7.3	1.7
$\kappa_t$	–	3.2	3.2
$\kappa_b$	0.99	0.89	0.44
$\kappa_\mu$	22	4.7	4.1
$\kappa_T$	2.5	1.3	0.60

**Preliminary** Fit Result with Forward Muon Tagging [%]

	3 TeV @ 1 ab <sup>-1</sup>	10 TeV @ 10 ab <sup>-1</sup>
$\kappa_W$	0.44	0.13
$\kappa_Z$	1.3	0.38
$\kappa_g$	2.4	0.68
$\kappa_\gamma$	4.0	1.1
$\kappa_{Z\gamma}$	–	–
$\kappa_c$	7.4	2.3
$\kappa_t$	–	–
$\kappa_b$	0.98	0.27
$\kappa_\mu$	22	5.3
$\kappa_T$	2.5	0.71